

**1.** Decide which of the four properties (reflexive, symmetric, transitive, antisymmetric) are true for the following relations.

- (i) the usual  $\leq$  among the real numbers;
- (ii) the usual  $<$  among the real numbers;
- (iii) the usual  $=$  among the real numbers;
- (iv)  $aRb$  if  $a$  and  $b$  have the same residue modulo 3 among the integers;
- (v)  $aRb$  if the reduced quotient  $\frac{a}{b}$  has odd denominator among the integers;
- (vi) the usual  $|$  (divisible) among the integers;
- (vii)  $aRb$  if  $a$  is the son of  $b$  among people;
- (viii)  $aRb$  if  $a$  and  $b$  have a border crossing among countries;
- (ix)  $aRb$  if we can travel from  $a$  to  $b$  on dry land among cities;
- (x) (in the last three the set is of all circles on the plane)  $c_1Rc_2$  if  $c_1$  and  $c_2$  meet;
- (xi)  $c_1Rc_2$  if  $c_1$  contains the centre of  $c_2$ ;
- (xii)  $c_1Rc_2$  if  $c_1$  contains  $c_2$  or  $c_2$  contains  $c_1$ .

**2.** Compute the following divisions with remainder:

- (i)  $5 : 1$
- (ii)  $1 : 5$
- (iii)  $-333 : 5$
- (iv)  $36357478585 : 10$
- (v)  $2^{12} + 1 : 2$
- (vi)  $3^{12} - 1 : 3$
- (vii)  $10^{12} : 9$

**3.**

- (i) Convert 26 to base 16, 8, 4, 2, 5 and 26!
- (ii) Convert 2025 to base 2, 8 and 16!
- (iii) What is the decimal (base 10) representation of the number  $120201_3$ ?